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Positron-Matter Collisions

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Low-Energy Positron Scattering

- Isolated collision between one target (atom or molecule) and one positron of known kinetic energy
- Only elastic scattering—stay below the energy threshold for electronic excitation of the target or for real positronium formation
- Local, energy-independent interaction potential based on physically-motivated approximations

Scattering Formulation

N-electron target and a colliding positron Consider the time-independent Schrödinger equation (T.I.S.E.) for an

$$\hat{\mathcal{H}}|\Psi> = E|\Psi>$$

where,

$$\hat{\mathcal{H}} = \hat{\mathcal{H}}_t + \hat{T}_p + \hat{V}_{int},$$

with,

- $\hat{\mathcal{H}}_t \equiv \text{N-particle Target Hamiltonian},$
- $\hat{T}_p \equiv \text{K.E. operator for the positron, and}$
- $V_{int} \equiv \text{positron-Target interaction operator.}$

Reduction of Scattering Formulation

complete set of target and scattering states, viz. We "reduce" the problem by expanding the (N+1)-particle ket in a

$$|\Psi>=\sum_{\gamma}F_{\gamma}\Phi_{\gamma}.$$

scattering of the positron $<\Phi_0|$ eventually leaves the one-particle T.I.S.E. for elastic Using this expansion in the T.I.S.E. and operating on the left with

$$\hat{T}_p|F_0>-\frac{k^2}{2}|F_0>=-\hat{V}_{sp}|F_0>.$$

Interaction Potential

positron and the molecular target can be represented as A local approximation to the interaction potential between a colliding

$$V_{sp}(\vec{r}_p) = V_{st}(\vec{r}_p) + V_{pol}(\vec{r}_p),$$

where the static potential is given by,

$$V_{st}(\vec{r}_p) = \left\langle \Phi_0(\vec{r_i}) \left| \hat{V}_{int} \right| \Phi_0(\vec{r_i}) \right\rangle,$$

with V_{int} representing the Coulomb interactions between the positron and the target and where $V_{pol}(\vec{r}_p)$ is the polarization potential.

Polarization Potential

The polarization potential is defined as the energy difference

$$V_{pol}(\vec{r}_p) = E^R(\vec{r}_p) - E^U(\vec{r}_p),$$

where the energy from the relaxed (distorted) target orbitals is

$$E^{R}(\vec{r}_{p}) = \left\langle \Phi^{R}(\vec{r}_{i}; \vec{r}_{p}) \left| \hat{\mathcal{H}}_{t} + \hat{V}_{int} \right| \Phi^{R}(\vec{r}_{i}; \vec{r}_{p}) \right\rangle_{d\vec{r}_{i}},$$

and the energy from the unrelaxed (ground state) orbitals is

$$E^{U}(\vec{r}_{p}) = \left\langle \Phi_{0}^{U}(\vec{r}_{i}) \left| \hat{\mathcal{H}}_{t} + \hat{V}_{int} \right| \Phi_{0}^{U}(\vec{r}_{i}) \right\rangle_{d\vec{r}_{i}}.$$

variational estimates of these energies using an LCAO:MO—SCF Quantum Chemistry code to provide by treating the projectile as an additional "proton" (located at \vec{r}_p) and In the adiabatic approximation, both $E^U(\vec{r}_p)$ and $E^R(\vec{r}_p)$ are calculated

Nuclear Attraction Integrals

attraction integrals that involve the positron as an additional "nucleus" The distortion of the molecular orbitals is driven by the nuclear

$$I_{i,j}^{NAI} = \langle \alpha_i(\vec{r}_e) | V(\vec{r}_e; \rho_{pos}) | \beta_j(\vec{r}_e) \rangle,$$

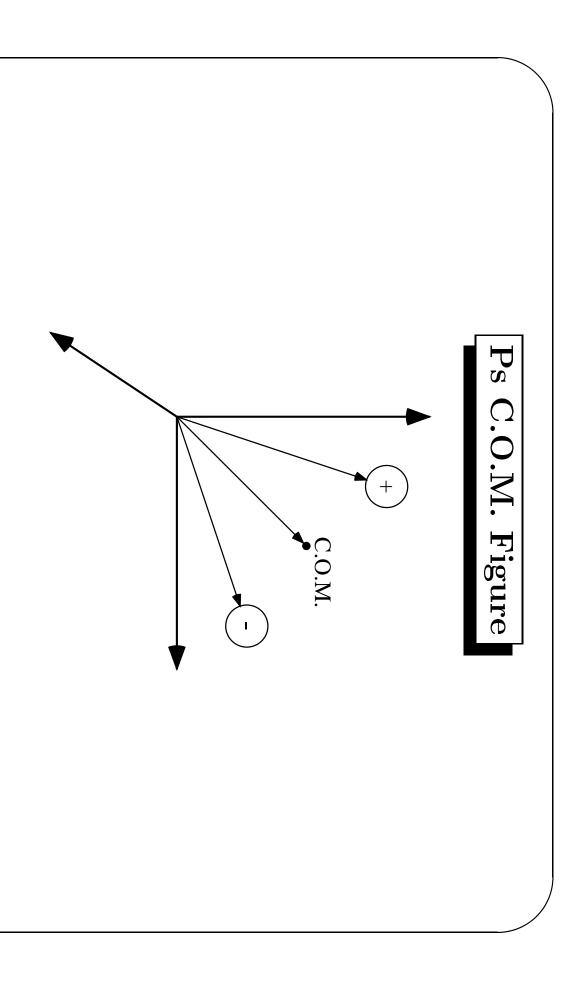
given as where the interaction V from a distribution of positive charge ρ_{pos} is

$$V(\vec{r}_e;
ho_{pos}) = \int d\vec{r} \,
ho_{pos}(\vec{r}) \, rac{-1}{|\vec{r}_e - \vec{r}|}.$$

appropriate for the positive charge distribution in a virtual H atom. For the adiabatic approximation, $\rho_{pos}(\vec{r}) = \delta(\vec{r} - \vec{r}_p)$, which is

Virtual Positronium

Positron Model (DPM). correct for virtual Ps. Thus, we refer to this scheme as the Distributed attraction integrals involving the positron with one that is more nearly replacing the delta function distribution of positive charge in the nuclear approximate the effect of this difference on the polarization potential by charge in a virtual H atom (see the figure on the following page). We can charge in a virtual Ps atom is not the same as the distribution of positive the positron and electron have equal masses, the distribution of positive much too attractive in the near-target region. The problem is that since The adiabatic approximation leads to a polarization potential that is



not localized at the C.O.M. of the atom.

Figure 1: Unlike the H atom, the positive charge in the Ps atom is

The Distributed Positron Model

polarization potential, including: potential that reduces to the correct long-range behavior of the distribution of positive charge in a Ps atom and lead to a polarization We have investigated several simple choices of ρ_{pos} that reflect the

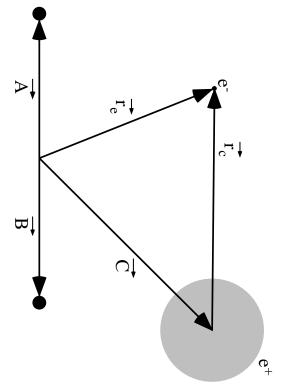
- Uniform Spherical
- $-R_p = 1.5 \text{ Bohr (Average radius of Ps atom)}$
- $-R_p = 1.0 \text{ Bohr (Maximum radial probability of Ps atom)}$
- H1S distribution
- STO-3G distribution

DPM Figure

For specificity, consider the following case:

- Diatomic target with nuclei at $ec{A}$ and $ec{B}$
- Additional "nucleus" (positron) with charge distribution ρ_{pos} located at

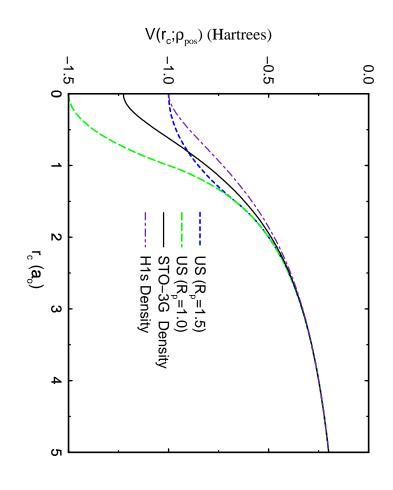
 $\vec{C} \equiv \vec{r_p}$



formation in the DPM. Figure 2: A distribution of positive charge simulates the effect of virtual Ps

DPM Distortion Interaction Figure

DPM Distortion Interactions



the DPM. Figure 3: The distortion interaction $V(\vec{r}_c; \rho_{pos})$ for various choices of ρ_{pos} in

Computing the Interaction Potential

systems, such as SF₆, remained out of reach. highly-optimized suite of codes (PATMOL) to perform these operations, larger computer resources is required. Even though we had written our own linear molecules to 1000's for non-linear molecules, a substantial amount of smooth interpolation of the polarization potential runs from 100's for atoms or location of the positron and since the number of points required to provide a for each of these points. Since most of the required integrals change with the near the target and then running a variational estimate of the system energy interaction potential involves fixing the positron at a large number of points Our method of calculating the polarization component of the positron-matter

- Larger Systems ⇒ More CPU Time
- Time to compute V_{pol} for Ar: 12 minutes (serial code)
- Time to compute V_{pol} for SF₆: 125 days (estimated)
- Larger Systems \Longrightarrow More Memory
- Larger Systems \implies More I/O

Solution—Concurrent Computing

Beowulf Cluster

Performance: 100's to 1000's of Megaflops

- Memory: Gigabytes

I/O: Distributed Across Multiple Nodes

Very Affordable Hardware

- Standard Software Available for Free

- Local Control

* Configuration Optimized for Problem

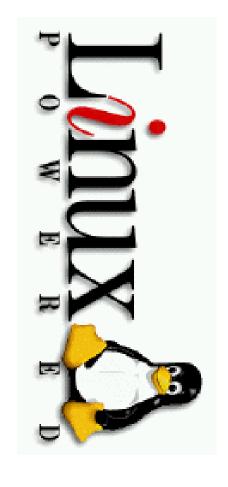
* No Sharing Required

Beowulf Quote

What is a Beowulf Cluster?

system. a high-bandwidth internal network, and the Linux operating clustered workstations based on commodity PC-class hardware, Beowulf is a project to produce the software for off-the-shelf

-Donald Becker



The PATMOL Codes

A Quantum Chemistry Program Suite written by

written by

Patrick J. Nichols

calculations. These codes have the following features: to compute polarization potentials for positron-molecule scattering PATMOL is a suite of programs written in C and C++ that we now use Texas Tech University

- A user-friendly interface
- Use of point group symmetry
- An integrals package based on the methods of McMurchie-Davidson [JCP **26**, 218-31 (1978)]
- A properties package
- Serial and Concurrent (MPI) versions